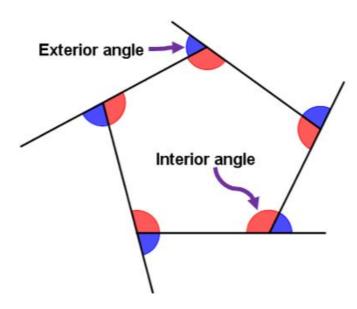
THE POLYGON ANGLE-SUM THEOREMS

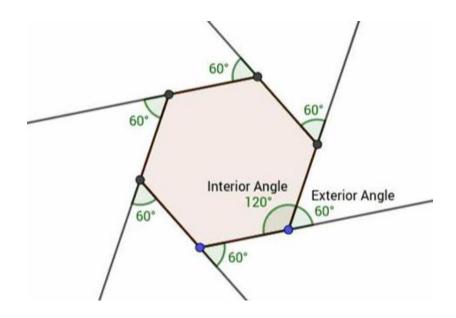
The Polygon Angle-Sum Theorems help us calculate the sum of the interior and exterior angles of polygons.



1. Interior Angle-Sum Theorem

The Interior Angle-Sum Theorem states:

The sum of the measures of the interior angles of a polygon with n sides are given by the formula:



Why does this work?

- A polygon with n sides can be divided into n−2 triangles by drawing diagonals from one vertex.
 - a. For example:
- A **triangle** (n=3) has 1 triangle. Its angle sum is $1.180 \circ = 180 \circ$
- A **quadrilateral** (*n*=4) can be divided into 2 triangles. Its angle sum is
- 2·180° =360°
- A **pentagon** (n=5) can be divided into 3 triangles. Its angle sum is $3.180 \circ = 540 \circ$
- 2. Since each triangle has a sum of 180° , the total sum for the polygon is the number of triangles $(n-2) * 180^{\circ}$.

Using the Formula

If you know the number of sides (*n*) of a polygon:

- 1. Subtract 2 from n.
- 2. Multiply the result by 180°

Example 1: Find the sum of interior angles of a hexagon (n=6).

Sum=
$$(6-2) \cdot 180 \circ = 4 \cdot 180 \circ = 720 \circ$$

Example 2: Find the measure of each interior angle of a regular octagon (n=8).

First, find the total sum of interior angles:

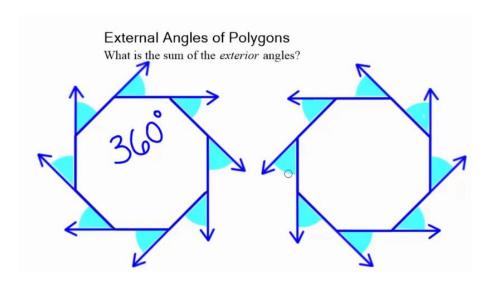
$$Sum = (8-2) \cdot 180 \circ = 6 \cdot 180 \circ = 1080 \circ$$

1. Divide the total sum by *n* to get the measure of one angle in a regular polygon:

2. Exterior Angle-Sum Theorem

The Exterior Angle-Sum Theorem states:

The sum of the measures of the exterior angles of a polygon, one at each vertex, is always 360°, regardless of the number of sides.



Why does this work?

- 1. The exterior angles of a polygon are the angles formed by extending one side of the polygon and measuring the angle between this extension and the adjacent side.
- 2. As you "walk around" the polygon, the exterior angles represent one complete rotation (a full 360.).

• This is true for any polygon, whether it has 3 sides or 100 sides.

Using the Theorem

You can find the measure of each exterior angle in a regular polygon by dividing 360° by the number of sides (n).

Example 1: Find the measure of each exterior angle of a regular hexagon (n=6).

Each exterior angle=360°/6 =60°

Example 2: If each exterior angle of a regular polygon measures 30°, how many sides does the polygon have?

So the polygon is a dodecagon (12 sides).

