## **Math Tutor**

## Weighted Averages and Atomic Mass

You have learned that the mass of a proton is about 1 u and that a neutron is only slightly heavier. Because atomic nuclei consist of whole numbers of protons and neutrons, you might expect that the atomic mass of an element would be very near a whole number. However, if you look at the periodic table, you will see that the atomic masses of many elements lie somewhere between whole numbers. In fact, the atomic masses listed on the table are *average* atomic masses. The atomic masses are averages because most elements occur in nature

as a specific mixture of isotopes. For example, 75.76% of chlorine atoms have a mass of 34.969 u, and 24.24% have a mass of 36.966 u. If the isotopes were in a 1:1 ratio, you could simply add the masses of the two isotopes together and divide by 2. However, to account for the differing abundance of the isotopes, you must calculate a *weighted average*. For chlorine, the weighted average is 35.45 u. The following two examples demonstrate how weighted averages are calculated.

## **Sample Problem**

A sample of naturally occurring silver consists of 51.839% Ag-107 (atomic mass 106.905 093 u) and 48.161% Ag-109 (atomic mass 108.904 756 u). What is the average atomic mass of silver?

To find average atomic mass, convert each percentage to a decimal equivalent and multiply by the atomic mass of the isotope.

$$0.518 39 \times 106.905 093 u = 55.419 u$$
  
 $0.481 61 \times 108.904 756 u = 52.450 u$   
 $107.869 u$ 

Adding the masses contributed by each isotope gives an average atomic mass of 107.869 u. Note that this value for the average atomic mass of silver is very near the one given in the periodic table.

A sample of naturally occurring magnesium consists of 78.99% Mg-24 (atomic mass  $23.985\,042\,u$ ), 10.00% Mg-25 (atomic mass  $24.985\,837\,u$ ), and 11.01% Mg-26 (atomic mass  $25.982\,593\,u$ ). What is the average atomic mass of magnesium?

Again, convert each percentage to a decimal and multiply by the atomic mass of the isotope to get the mass contributed by each isotope.

```
0.7899 \times 23.985\ 042\ u = 18.95\ u
0.1000 \times 24.985\ 837\ u = 2.499\ u
0.1101 \times 25.982\ 593\ u = 2.861\ u
24.31\ u
```

Adding the masses contributed by each isotope gives an average atomic mass of 24.31 u.

## **Practice**

- **1.** Rubidium occurs naturally as a mixture of two isotopes, 72.17% Rb-85 (atomic mass 84.911 792 u) and 27.83% Rb-87 (atomic mass 86.909 186 u). What is the average atomic mass of rubidium?
- **2.** The element silicon occurs as a mixture of three isotopes: 92.22% Si-28, 4.69% Si-29, and 3.09% Si-30. The atomic masses of these three isotopes are as follows: Si-28 = 27.976926 u, Si-29 = 28.976495 u, and Si-30 = 29.973770 u.

Find the average atomic mass of silicon.